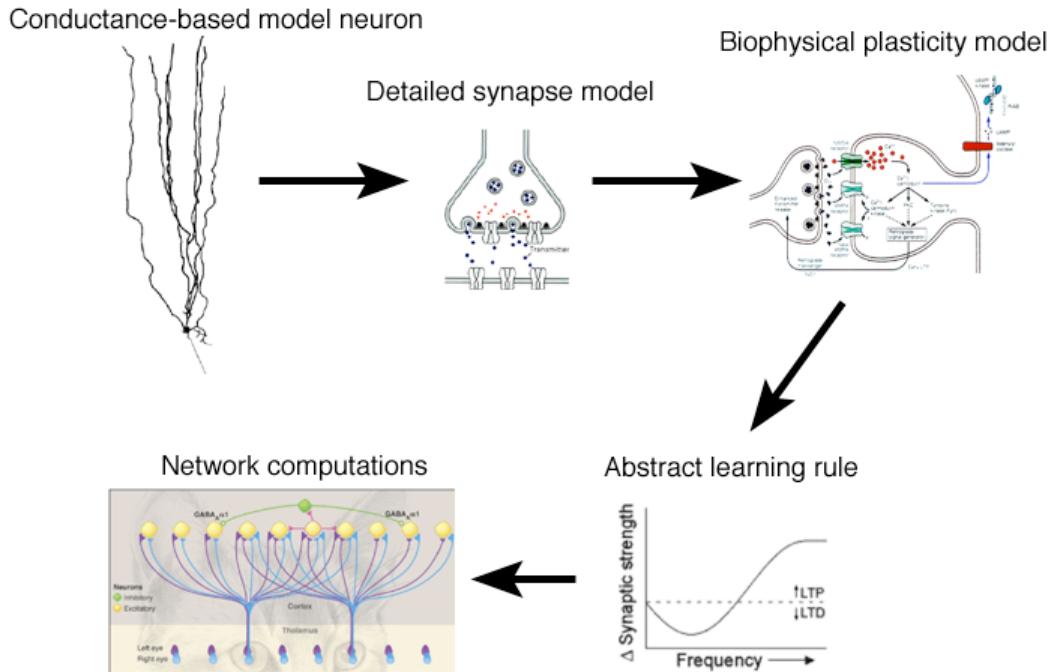


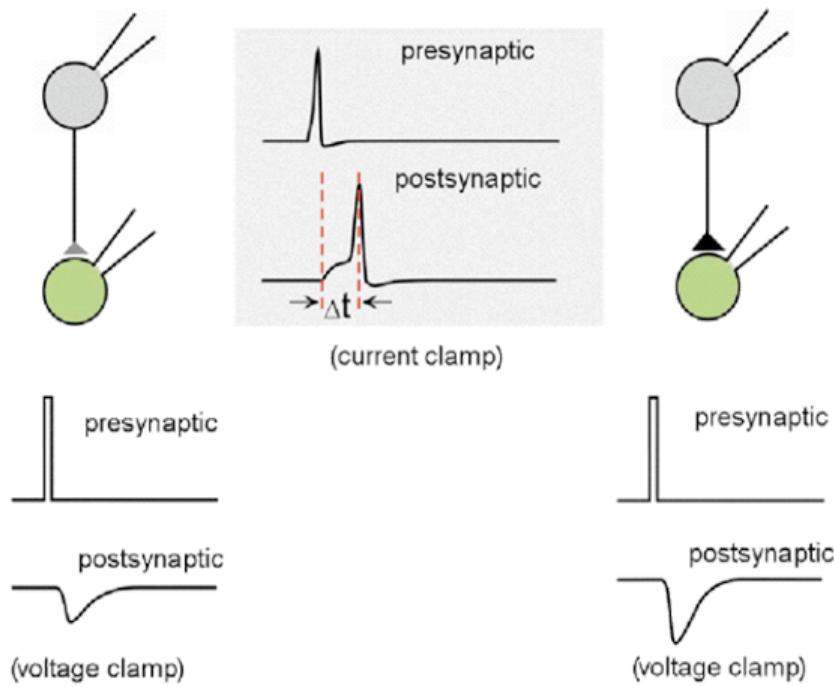
Simplified models of synaptic plasticity



Course website: <http://www.bme.ogi.edu/BME665/>

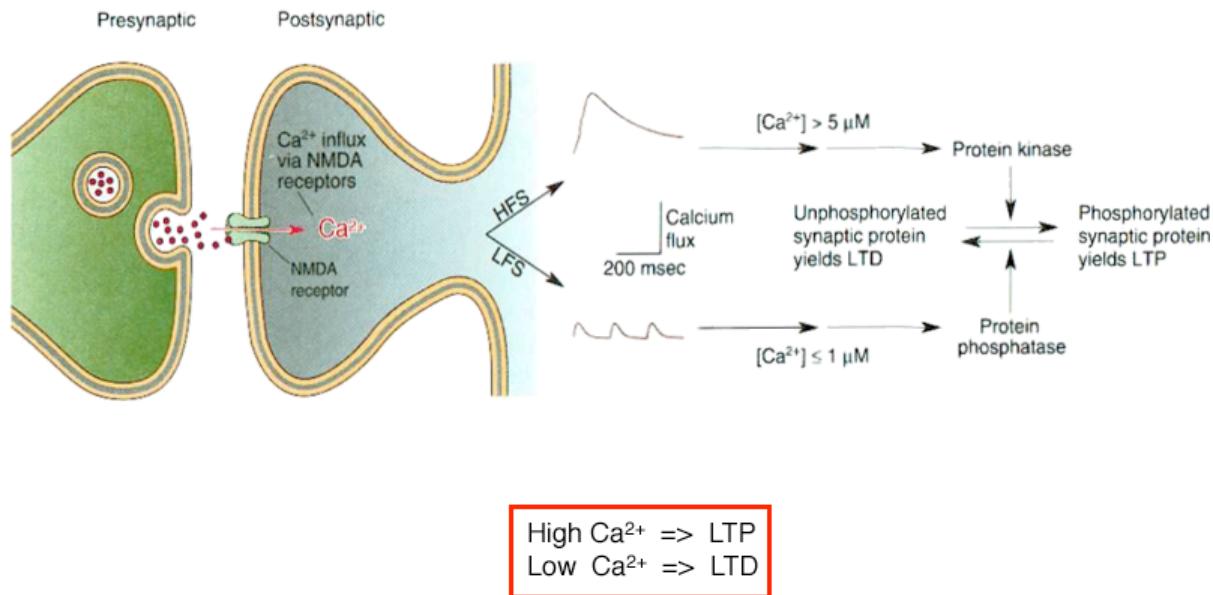
00_title.psd

Spike-Timing Dependent Plasticity (STDP)



00a_stdp_induct.psd

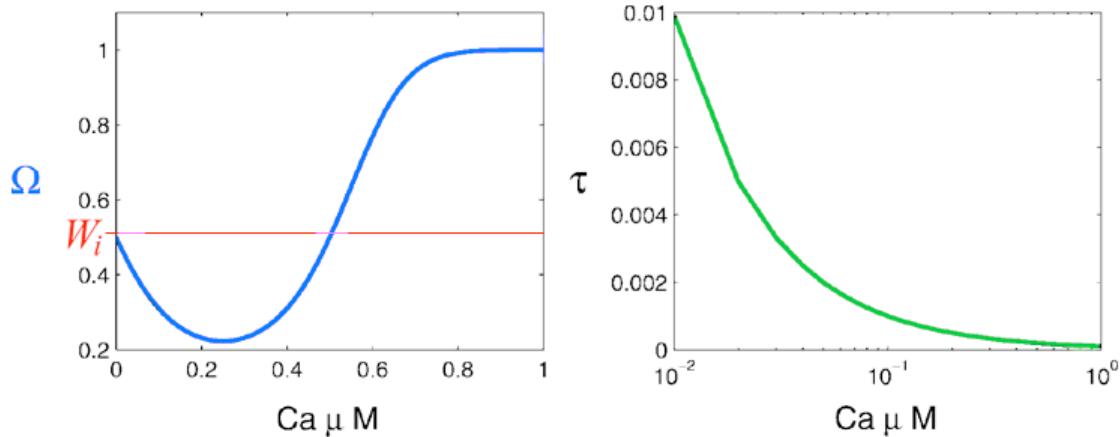
Calcium Concentration Determines Direction of Synaptic Plasticity



01_caDepPlast.psd

Simplified Model of Calcium-Dependent Plasticity

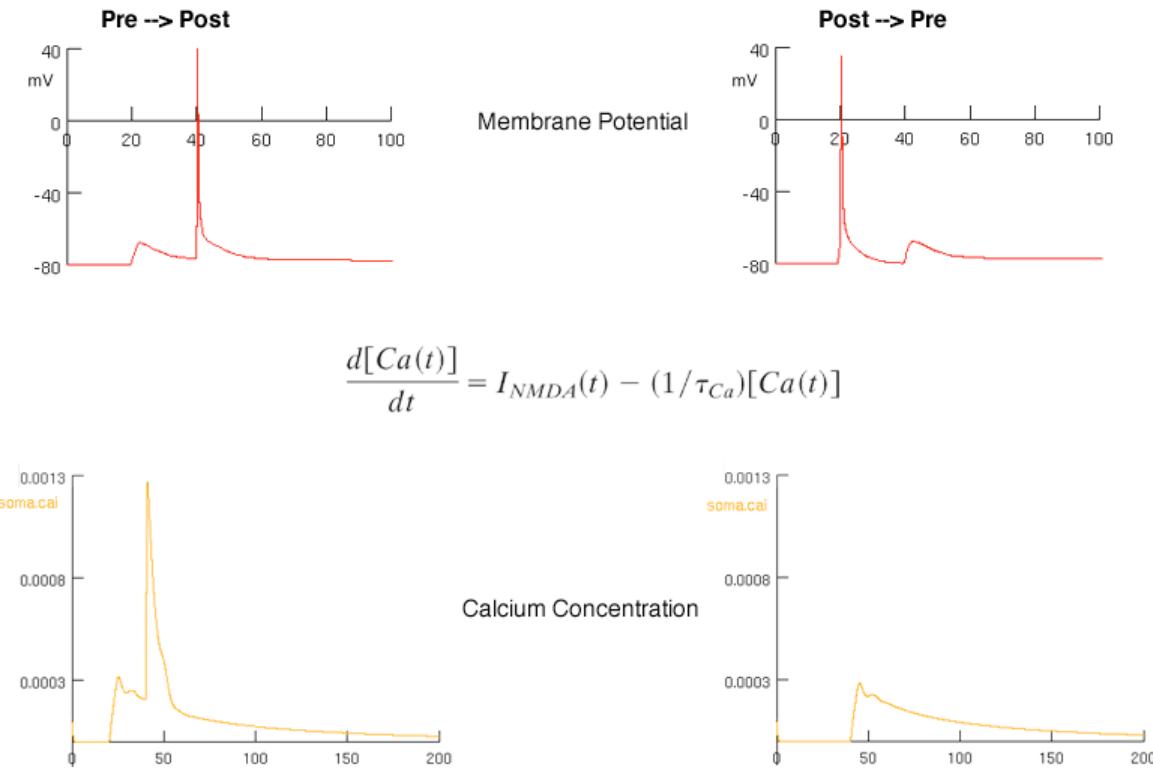
$$\dot{W}_i(t) = \frac{1}{\tau([Ca]_i)} (\Omega([Ca]_i) - W_i)$$



Lisman (1989), Shouval (2002)

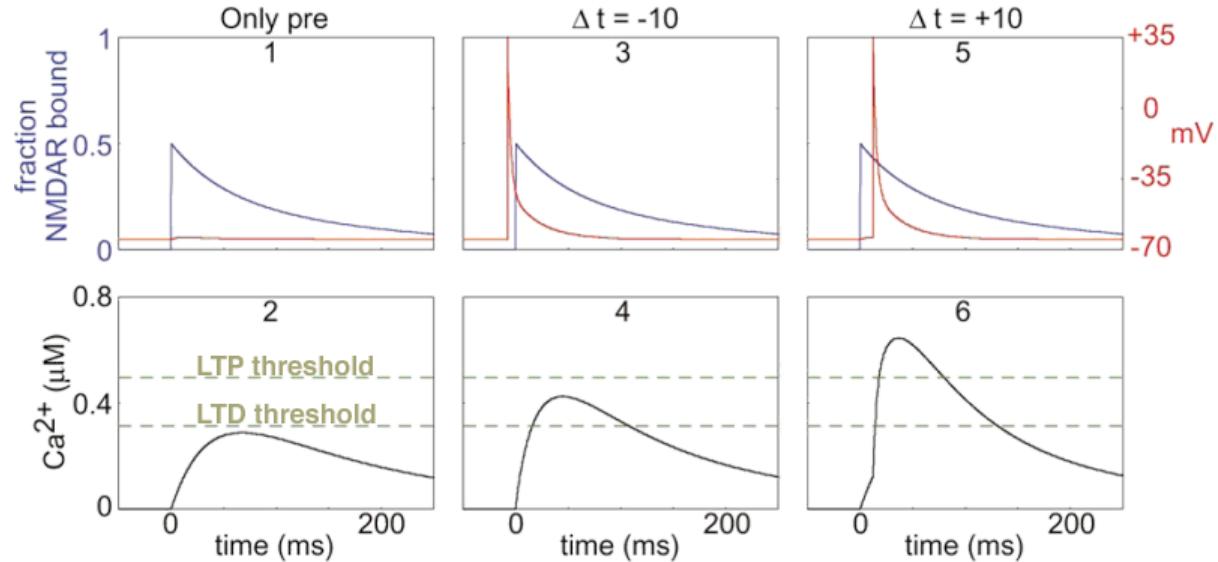
02_CaPlastEq.psd

Spike Order Controls Calcium Concentration



03_order.psd

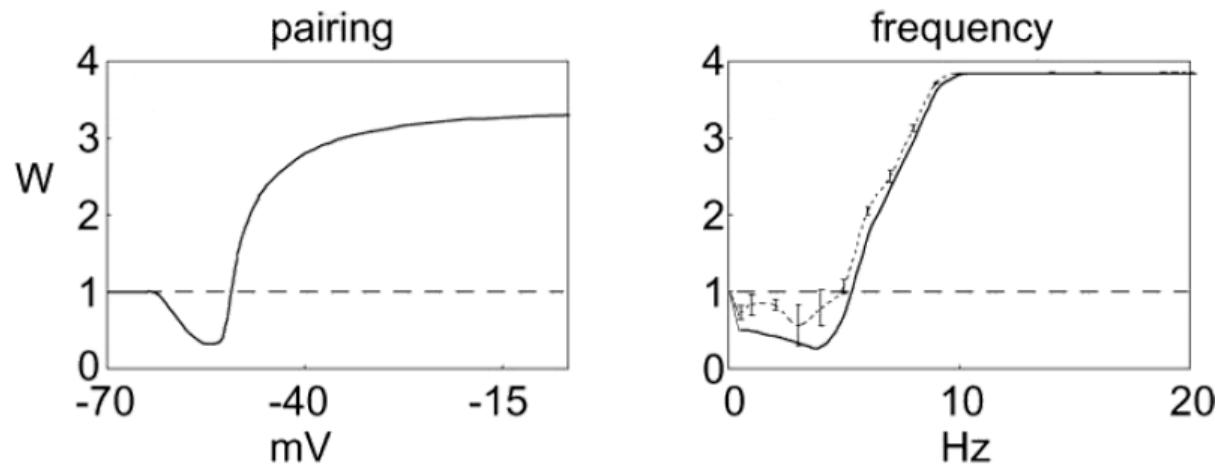
Calcium Threshold for Synaptic Plasticity Can Predict Effects of Spike-Pairing



Shouval (2002)

04_Ca_LTP.psd

Calcium Model Prediction of Frequency Dependency

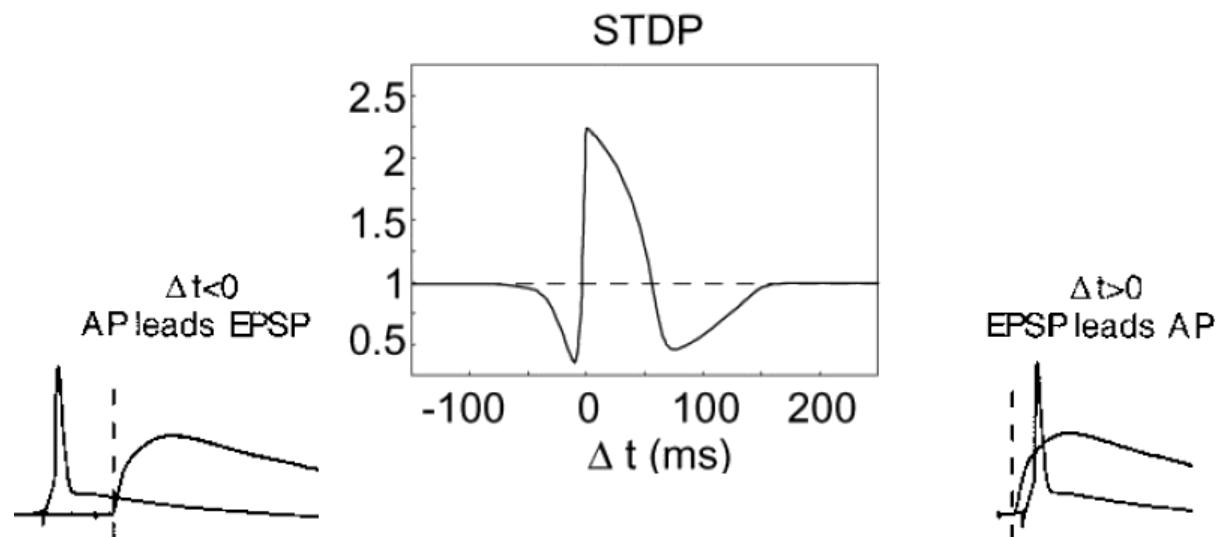


Consistent with the BCM model

Shouval (2002)

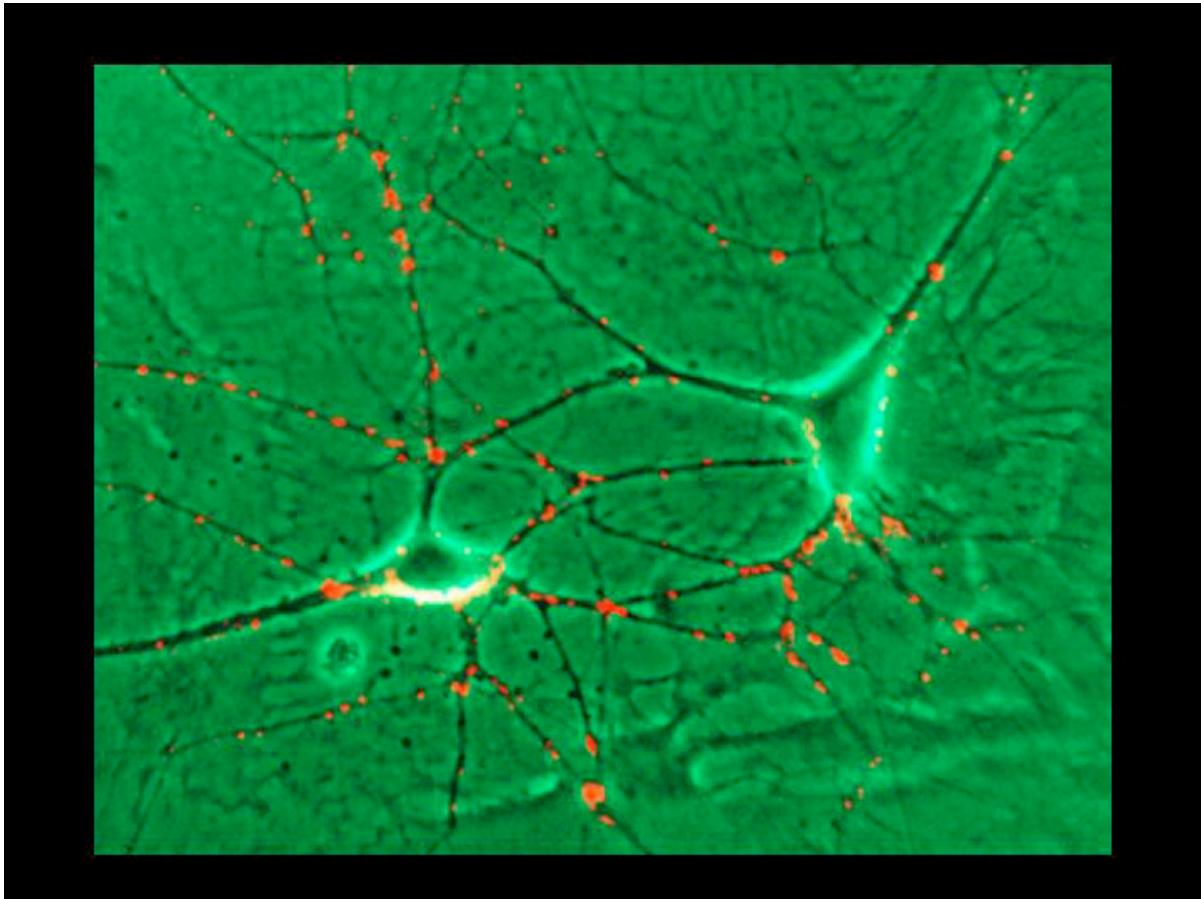
05_freqDep.psd

Calcium Model Prediction of Spike-Timing Dependent Plasticity

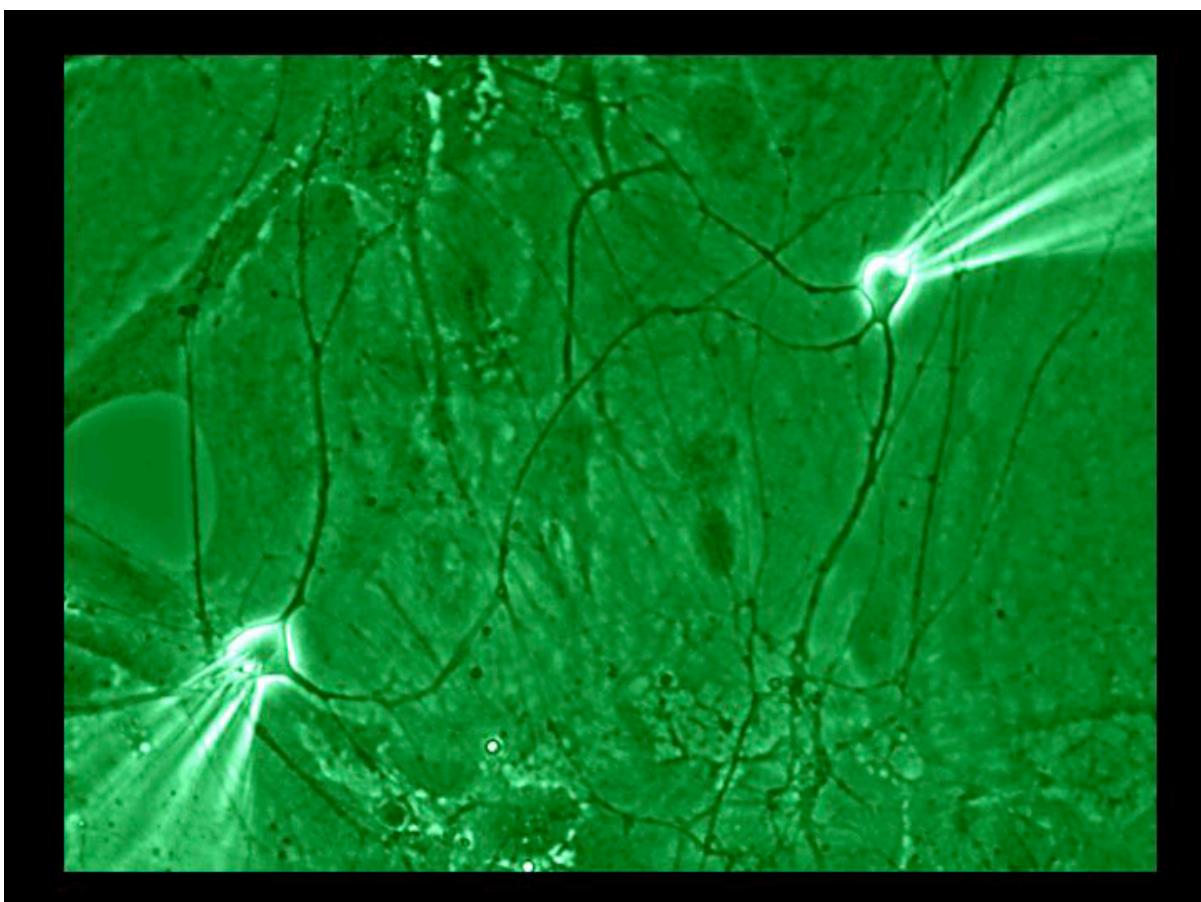


Shouval (2002)

06_Ca_stdp.psd

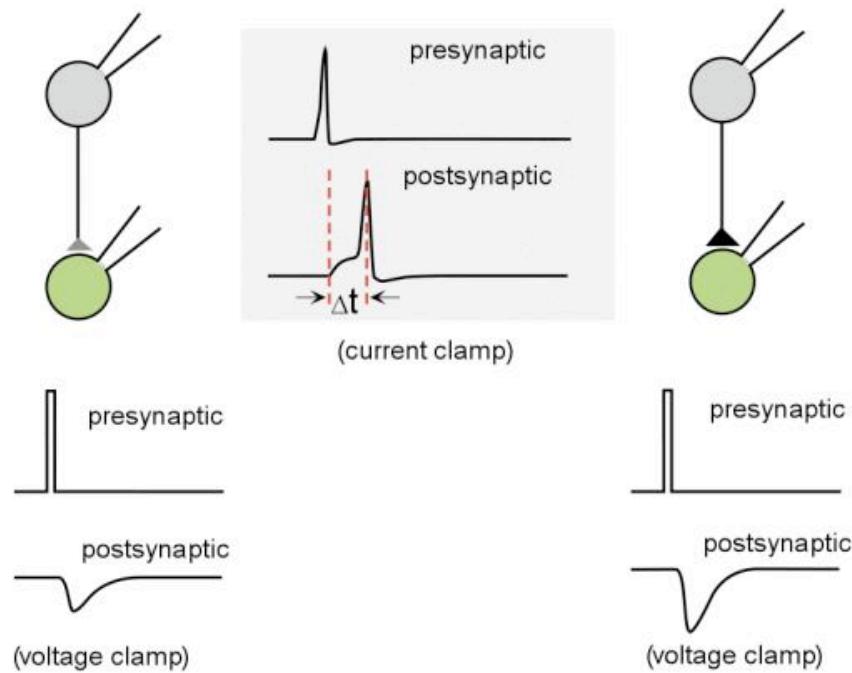


07a.jpg

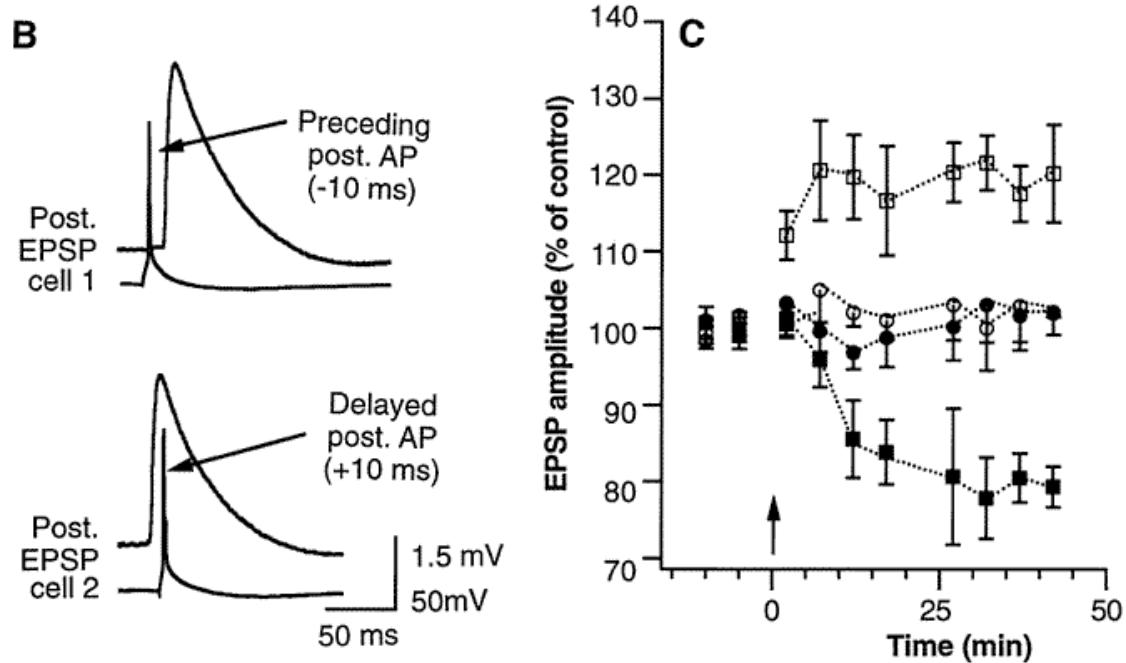


07b.jpg

Experimental paradigm -- correlated pre- and postsynaptic spiking



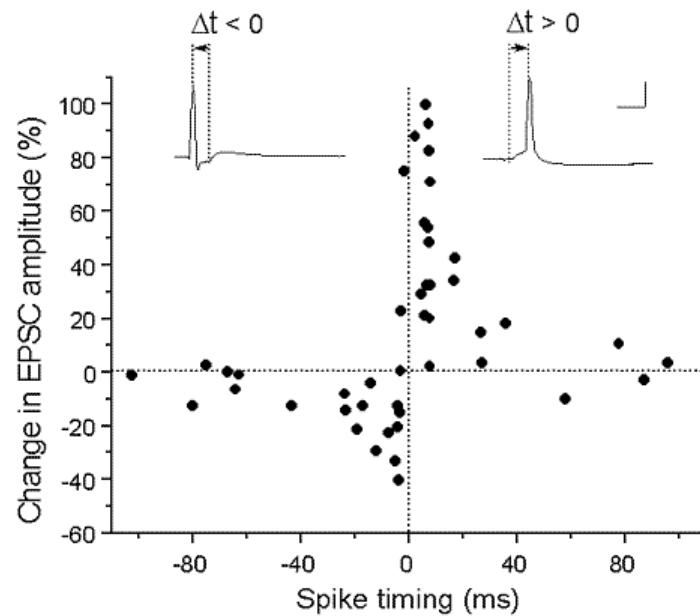
08.jpg



Markram et al. 1997

09.gif

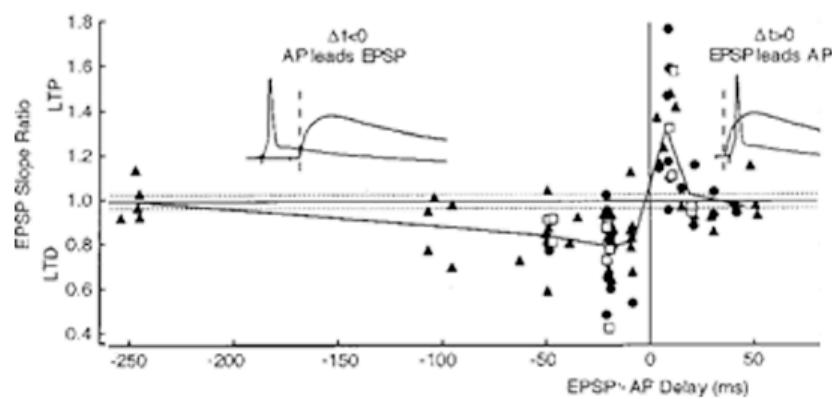
Anti-Symmetric STDP Learning Rule



Bi (1998)

10_BiRule.psd

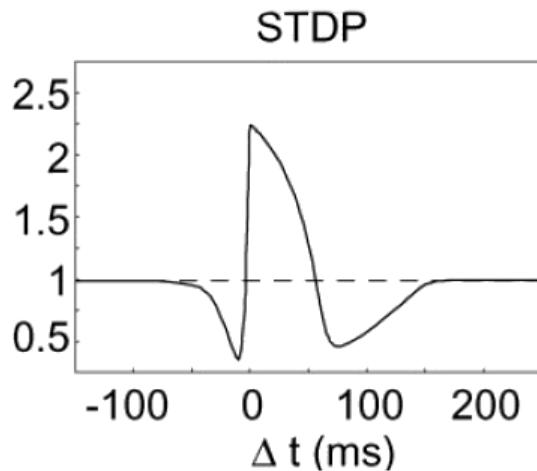
Long Interval of LTD



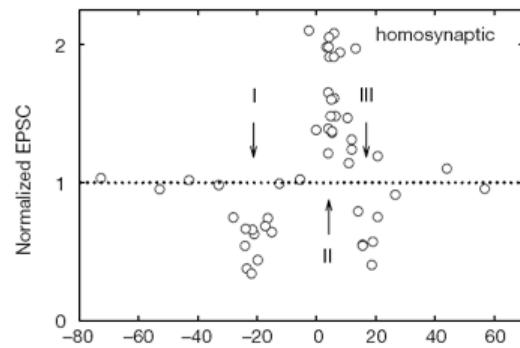
Feldman (2000)

11_feldmanRule.psd

Empirical Agreement with Calcium Model Prediction?

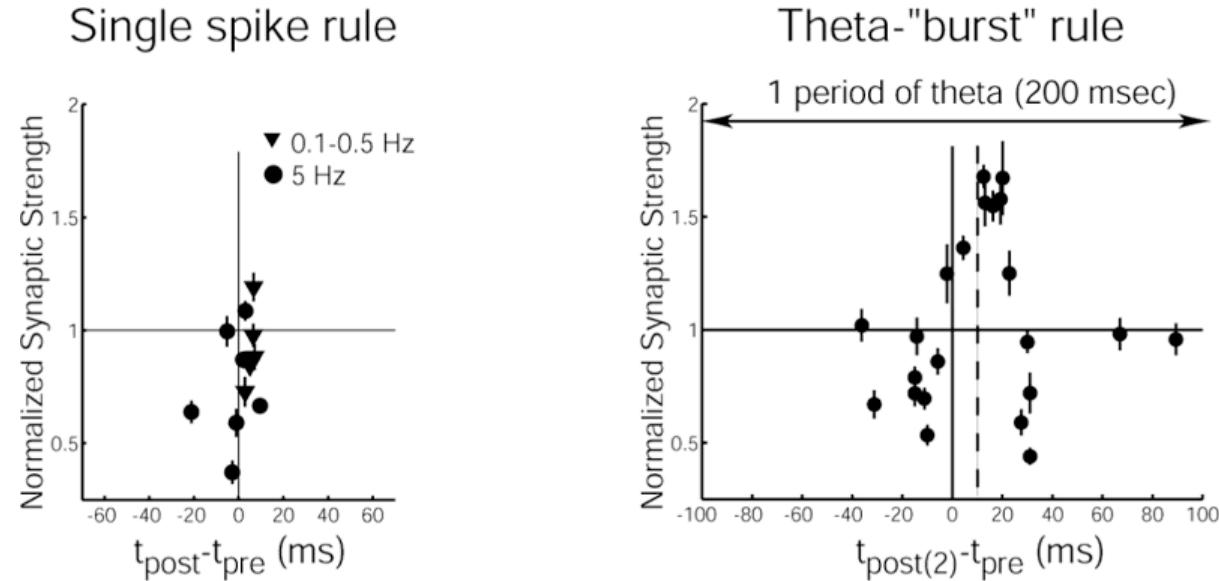


Shouval (2002)

Nishiyama (2000)
Hippocampus slice

12_Ca_stdp2.psd

Hippocampus Slice STDP with Burst-Pairing

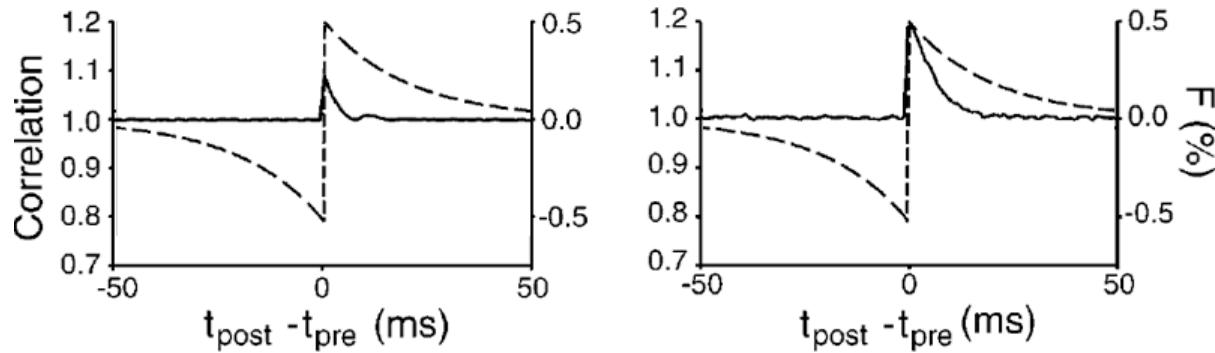


SS Wang, et al. (2004)

13_burstSTDP.psd

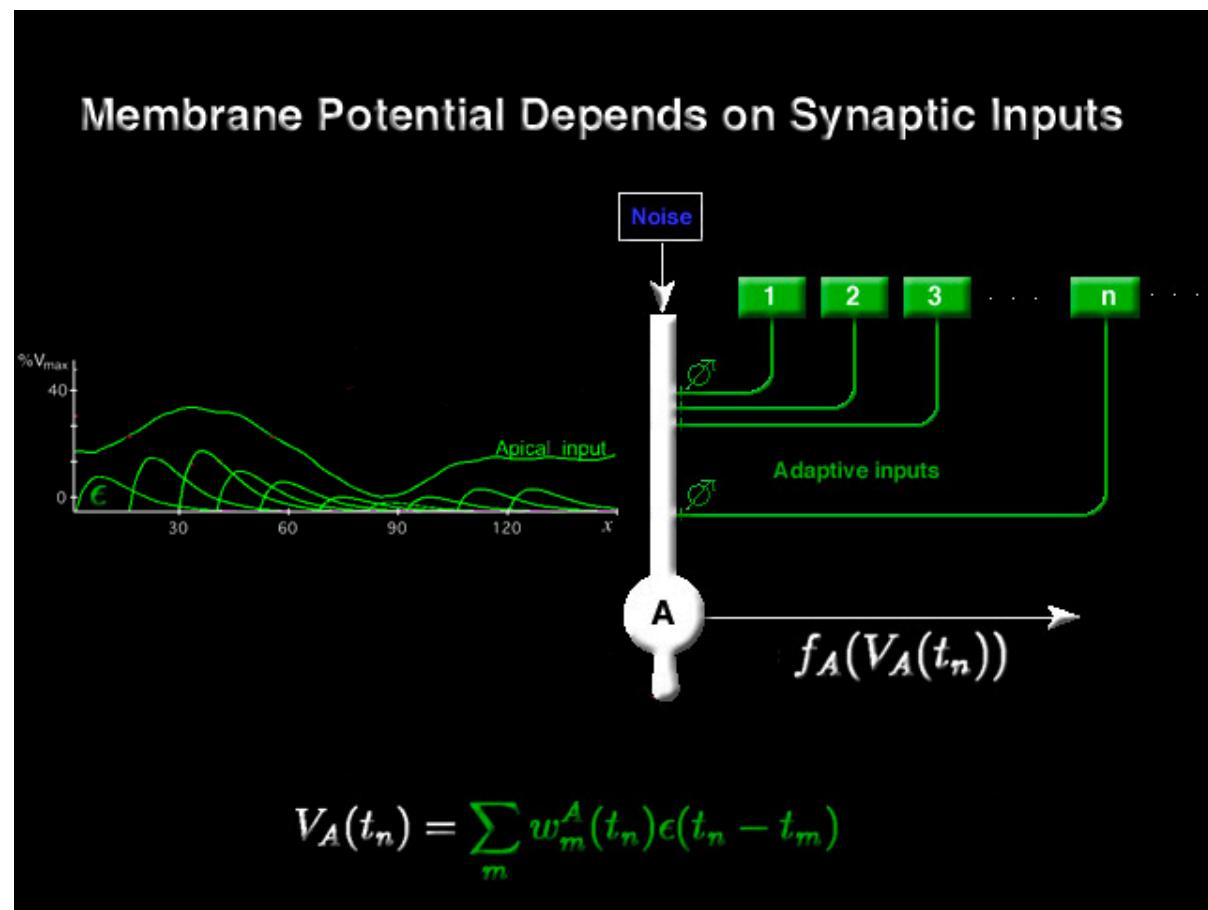
Competitive STDP Model

$$F(\Delta t) = \begin{cases} c_P e^{-|\Delta t|/\tau_P} & \text{if } \Delta t > 0 \\ -c_D e^{-|\Delta t|/\tau_D} & \text{if } \Delta t < 0 \end{cases}$$



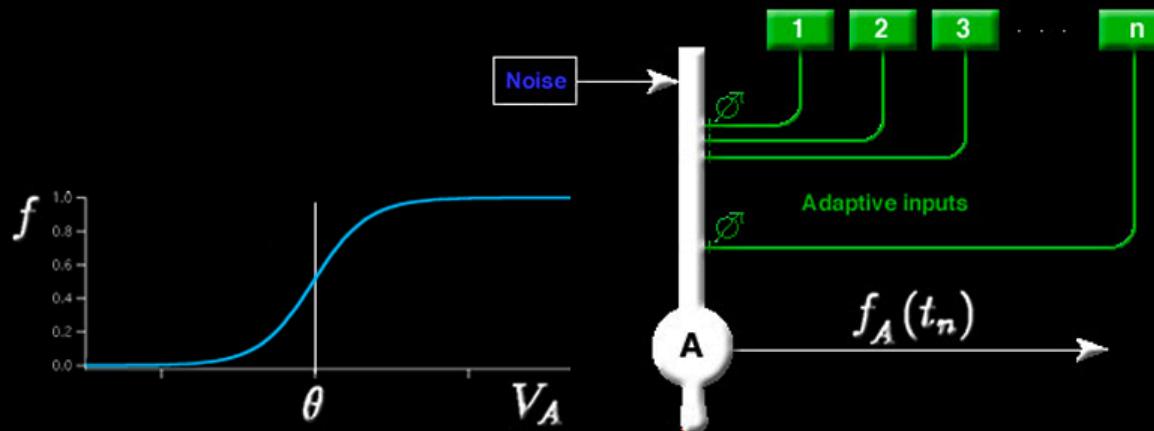
Song & Abbott (2000)

14_songRule.psd



15_Module.psd

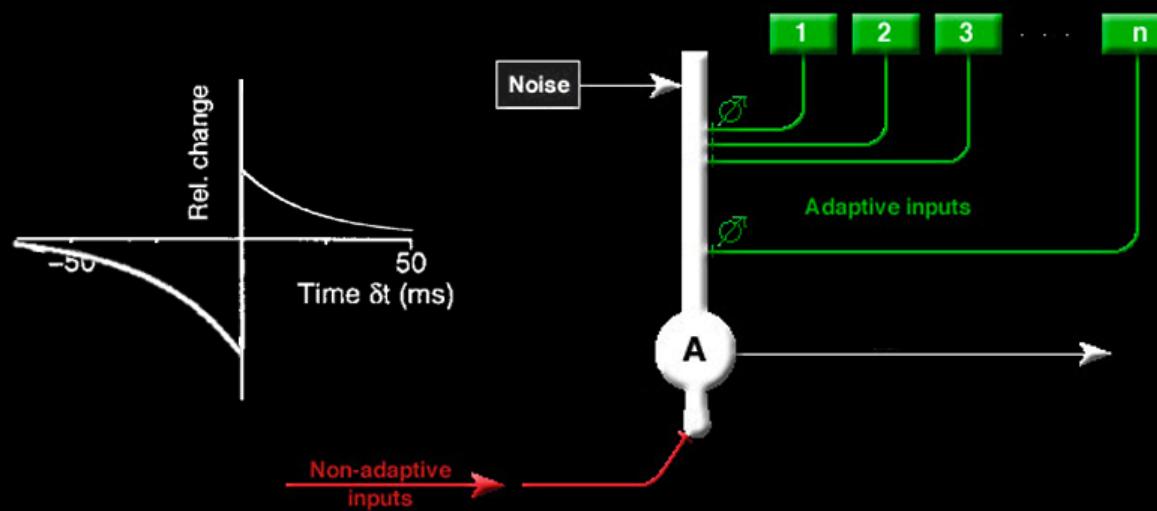
Spike Probability Depends on Membrane Potential



$$f_A(t_n) = f_A(V_A(t_n)) = \frac{1}{1 + \exp[-\mu(V_A(t_n) - \theta)]}$$

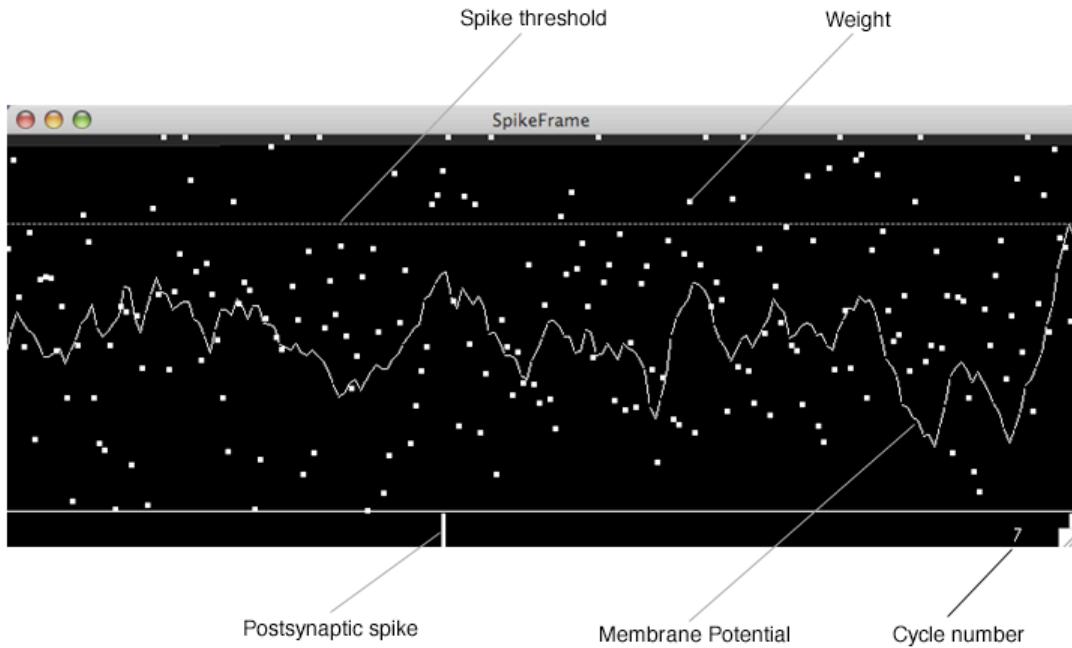
15b_Module.psd

Hebbian STDP with Dominant LTD Random Input Timings



17_feldmanSimul.psd

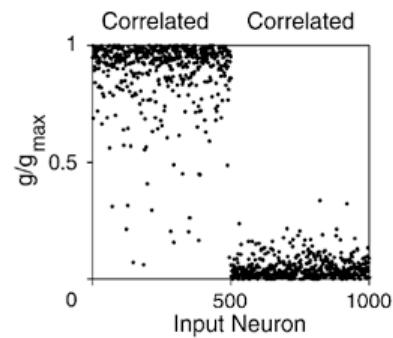
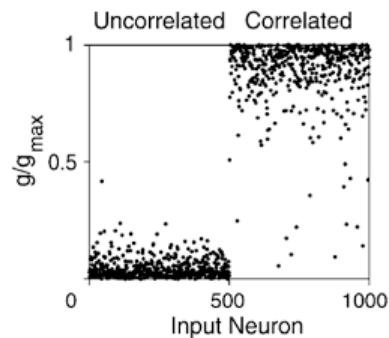
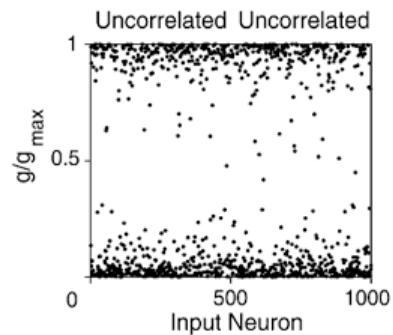
STDP Simulation



16_sim.psd

Competitive STDP Model

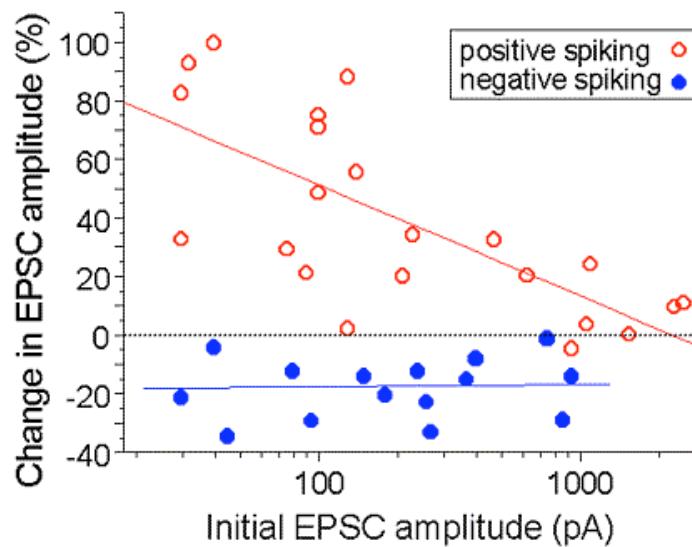
$$F(\Delta t) = \begin{cases} c_p e^{-|\Delta t|/\tau_p} & \text{if } \Delta t > 0 \\ -c_D e^{-|\Delta t|/\tau_D} & \text{if } \Delta t < 0 \end{cases}$$



Song & Abbott (2000)

18_competition.psd

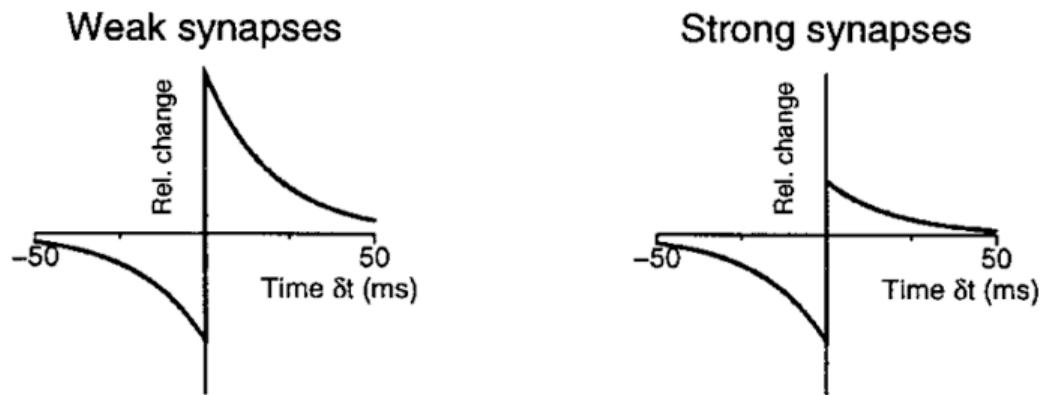
Dependence on initial synaptic strength



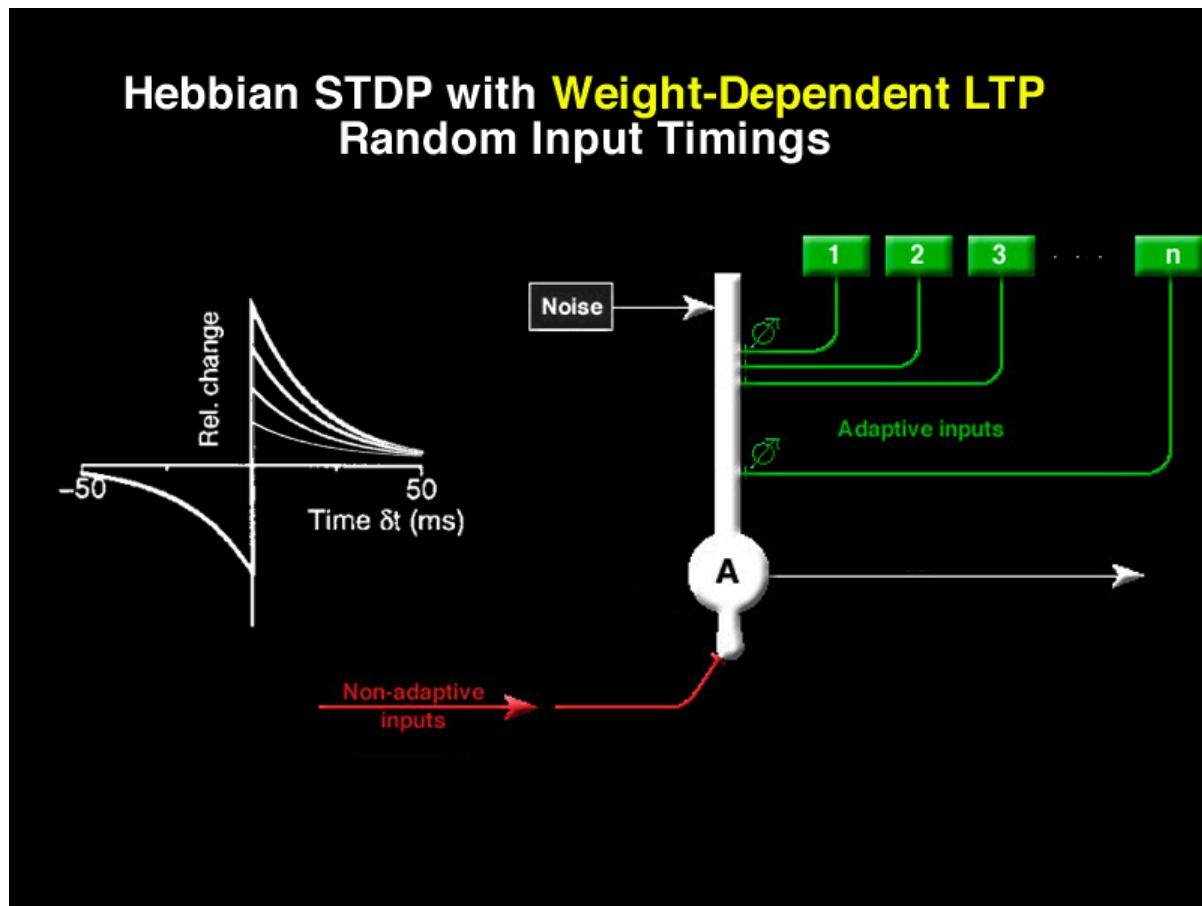
19.gif

Stable STDP Model

$$F(\Delta t) = \begin{cases} c_P e^{-|\Delta t|/\tau_P} & \text{if } \Delta t > 0 \\ -c_D w e^{-|\Delta t|/\tau_D} & \text{if } \Delta t < 0 \end{cases}$$

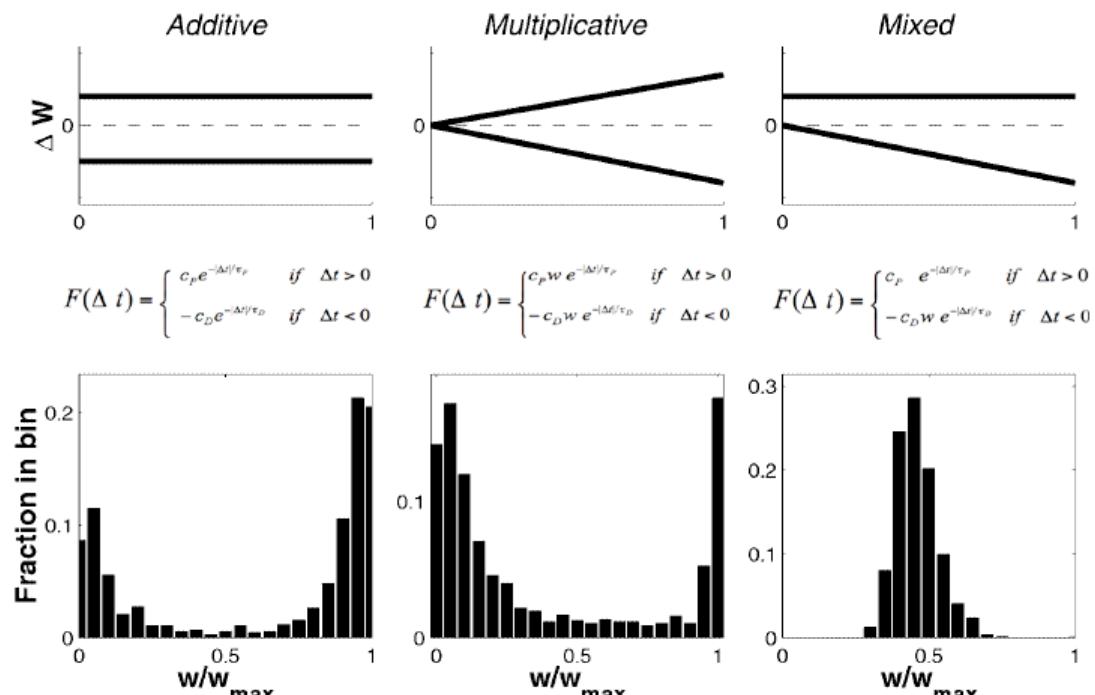


van Rossum et al. (2000)



21_biSimul.psd

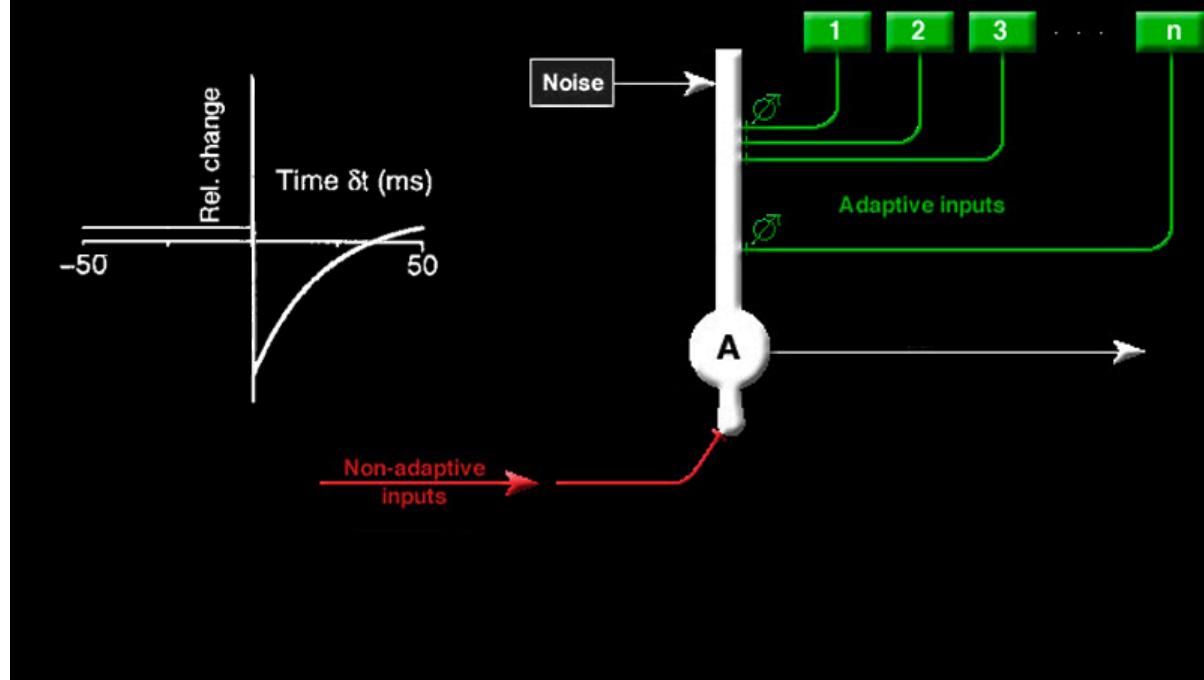
Additive vs. Multiplicative STDP Learning Rules



Kepecs, et al. (2002)

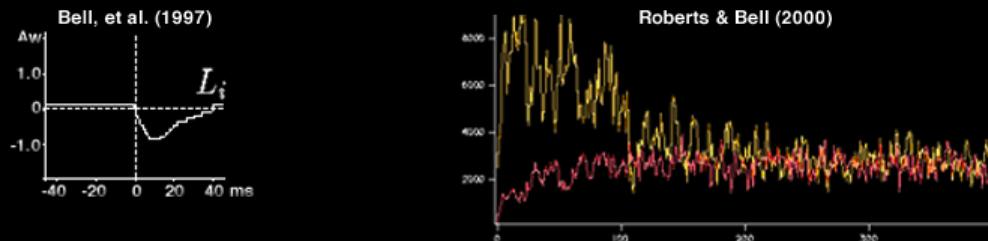
22_distrib.psd

Anti-Hebbian STDP with Non-associative LTP Random Input Timings



23_bellSimul.psd

Learning Dynamics Have Fixed Points



$$\langle \Delta w_i(x_n, t) \rangle = \alpha - \beta \sum_m L_i(x_m - x_n) f_b(x_m, t) \quad \sum_n L(x_n) = 1$$

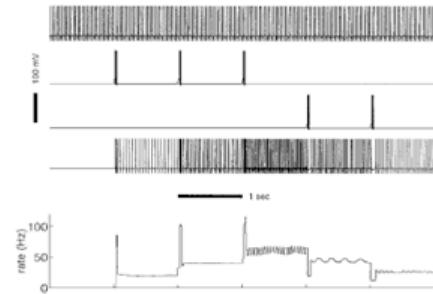
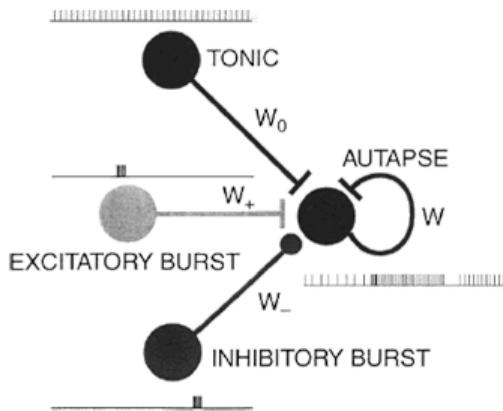
$$\langle \Delta w_i(x_n, t) \rangle = 0 \quad \Rightarrow \quad 0 = \alpha - \beta \sum_m L_i(x_m - x_n) \hat{f}$$

$$\boxed{\hat{f} = \alpha / \beta}$$

$$f(x_n, t) \rightarrow \hat{f} = f(\hat{V}) \text{ as } t \rightarrow \infty$$

24_FixedPt.psd

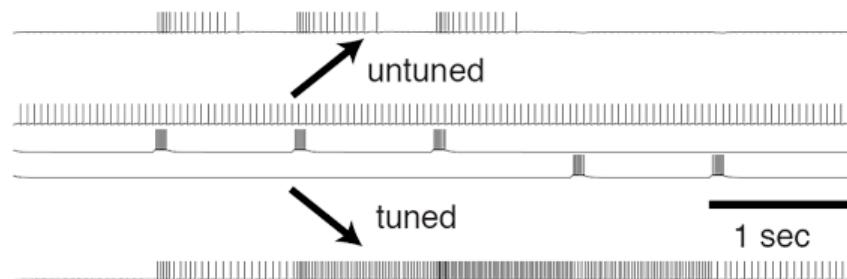
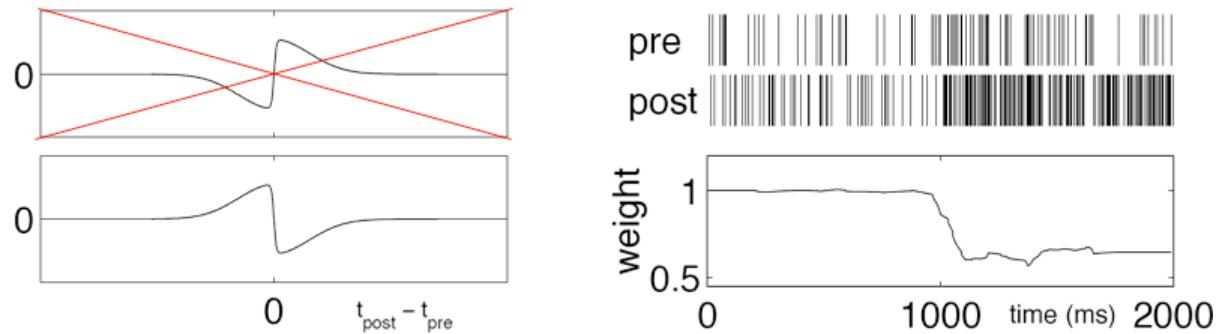
Neural Integrator



Seung, et al. (2000)

25_autopase.psd

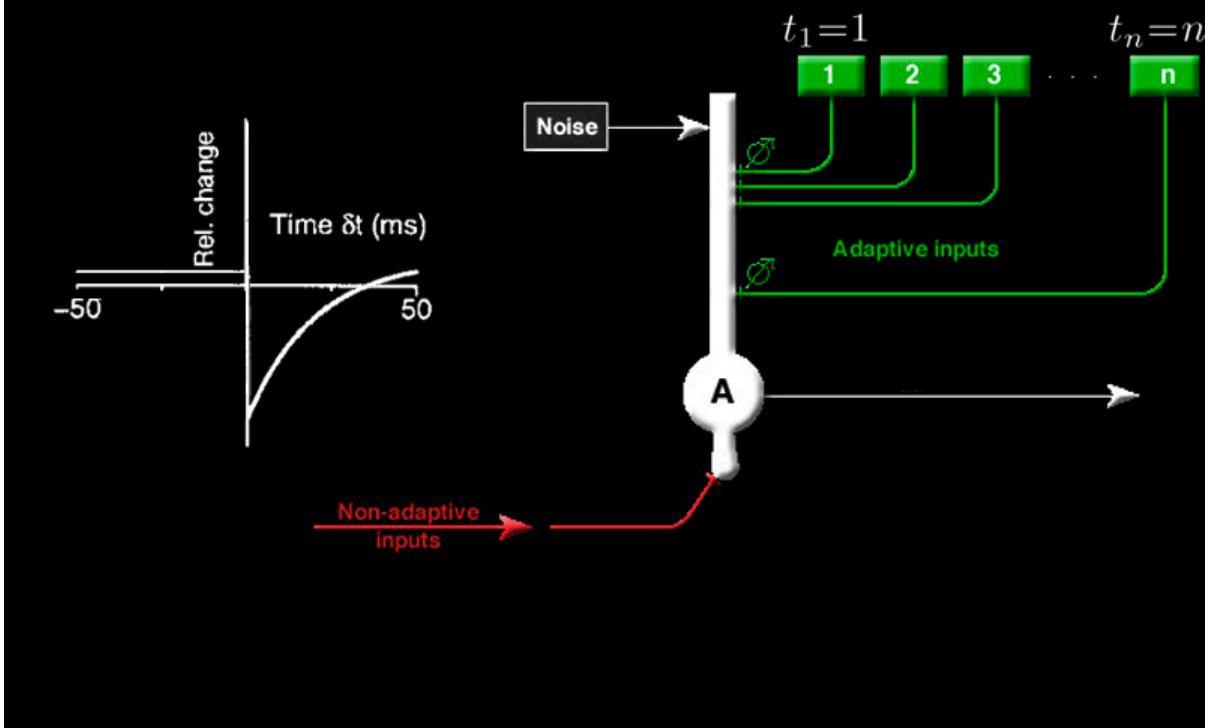
Tuning the Neural Integrator



Xie & Seung (2000)

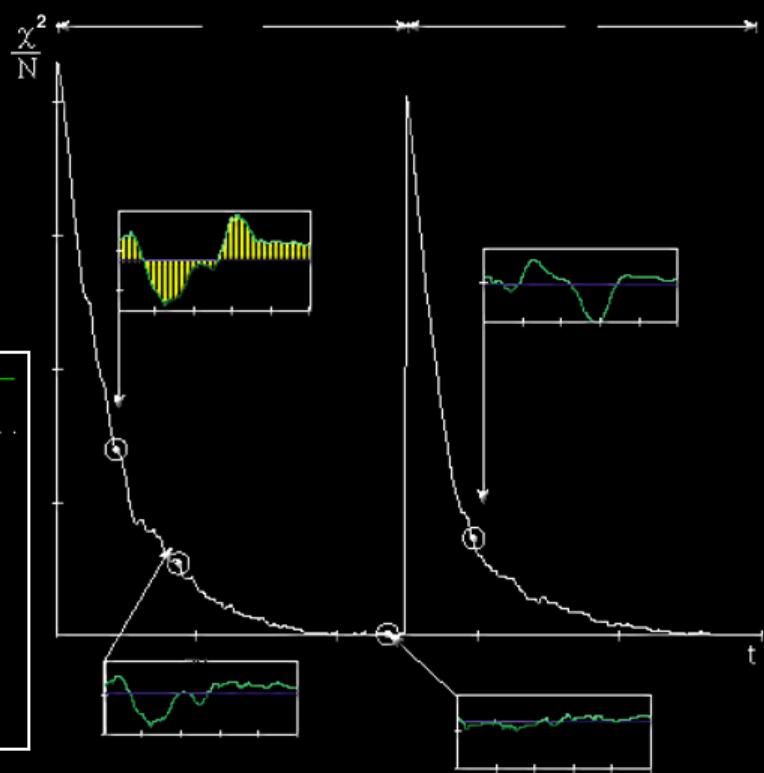
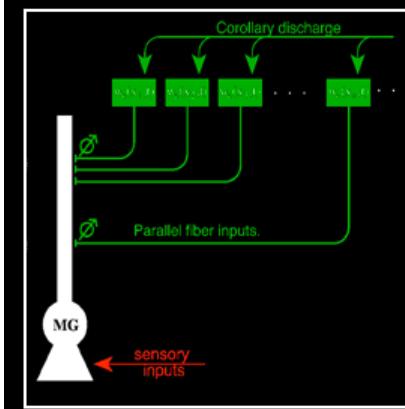
26_autopaseTune.psd

Anti-Hebbian STDP with Non-associative LTP Delay-line Input Timings



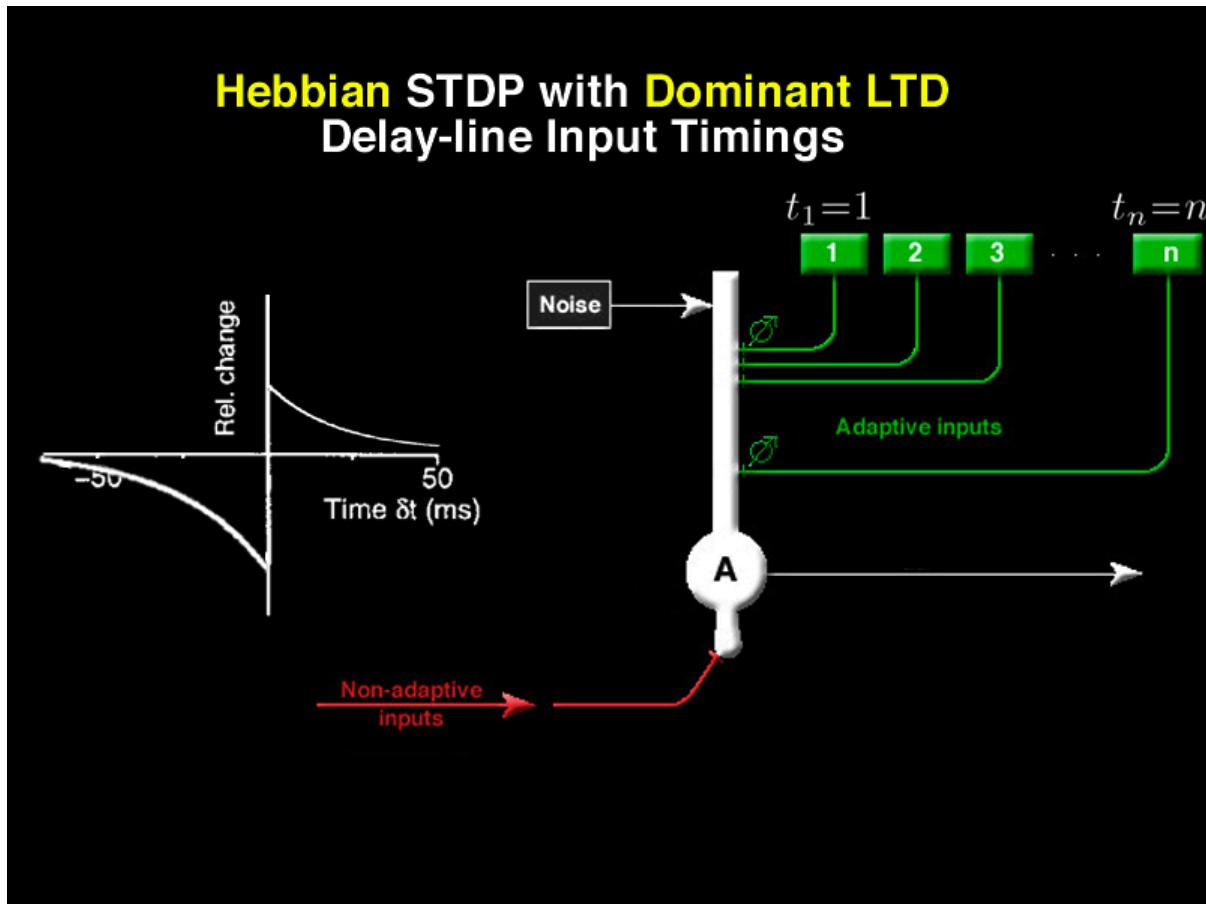
27_bellSimul2.psd

Expectation cancellation cancellation by the cerebellum-like algorithm.

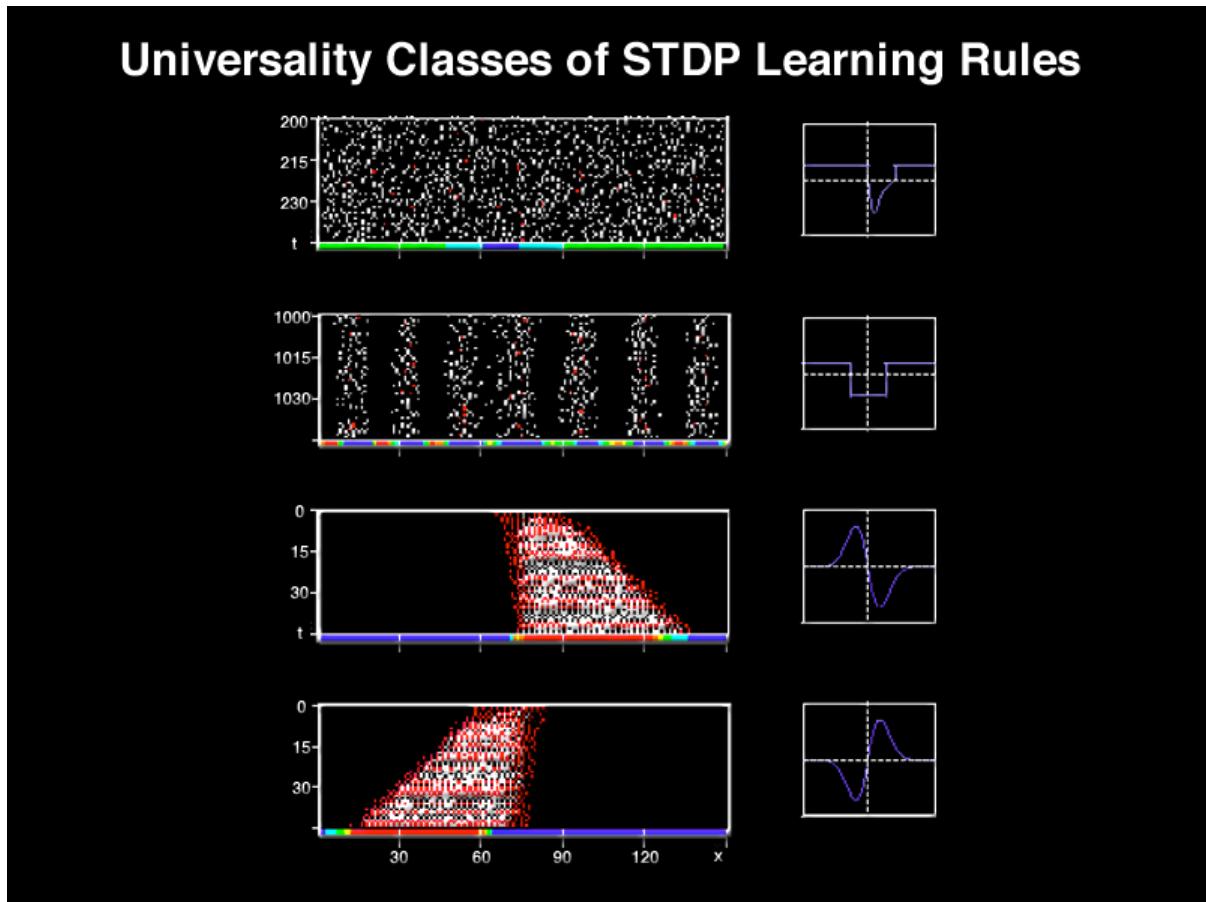


$$\frac{\chi^2}{N} = \frac{1}{N} \sum_{d=1}^N \frac{(\text{Average membrane potential} - \langle \text{Average membrane potential} \rangle)^2}{\langle \text{Average membrane potential} \rangle}$$

28_chi.psd



29_feldmanSimul2.psd



30_classesSTDP.psd